Traffic Blocking Theory for Data Services
## Executive Summary

1

## Background

2

## Traffic Blocking Analysis Methodology

4

### Traffic Blocking Theory Analysis and Typical Results

- Definition and Calculation Method of Session-level Hard Experience Blocking .................................................. 6
- Definition and Calculation Method of Session-level Soft Experience Blocking ................................................... 7
- Definition and Calculation Method of Packet Delay Blocking ........................................................................... 8
- Typical Results of Experience Blocking ........................................................................................................... 9
- Experience Blocking Calculation SDK ........................................................................................................... 10

## Traffic Blocking Theory Application

- Application 1: System Capacity Adjustment Method Based on Traffic Volume Requirements .......................... 11
- Application 2: System Capacity Adjustment Method Based on Experience Blocking Analysis ..................... 12

## Future Development

12
Executive Summary

As mobile broadband (MBB) networks, such as 4G networks, are rapidly deployed, the time spent watching video content and the traffic consumption overall increases significantly. No mature blocking theory is applicable to MBB networks oriented to user experience. Huawei mLAB of Wireless X Labs, Future Network Theory Lab of 2012 Labs, and some universities around the world jointly proposed a new traffic blocking theory for MBB data services, and formulated an experience blocking table (EB table) based on live-network data analysis, theoretical analysis, and simulation. The EB table can be used to evaluate the experience blocking status of users in the system based on system capacity, traffic modeling, and single-user bandwidth requirements. It can also be used to plan system capacity through theoretical analysis and simulation according to the experience blocking targets.
In 1909, Danish mathematician Agner Krarup Erlang, proposed a traffic blocking probability theory and this theory has been widely applied to voice networks. The theory is used for network simulation, planning of system capacity, and call blocking probability analysis on the live network. In the Erlang B formula, new incoming calls are blocked when all channels are occupied. In the Erlang C formula, new incoming calls can be queued until there are available channel resources when all channels are occupied. This does not affect users with ongoing services in the system.

Both the Erlang B and Erlang C formulas are not applicable to data services on MBB networks. Users performing data services in subhealth mode access the system. The new users will affect the experience of current users. If the number of concurrent users is greater than the number of users planned for the system, the experience of all concurrent users will deteriorate. For example, users performing video services experience video stalling (non-ABR) or video quality deterioration (ABR). Users downloading files or browsing the web experience a longer delay.
In the Erlang B formula, call arrivals following a Poisson distribution are considered. This is applicable to voice services. However, MBB data service arrivals often follow a long-tailed distribution (power-law distribution). That is, a large number of calls arrive in a short period of time. A small number of calls occupy a large amount of channel capacity.

Call arrivals following a Poisson distribution or a power-law distribution will result in a large number of concurrent sessions, instantaneously decreasing user-perceived throughput. Such situations exist on both light-load and heavy-load networks. Therefore, channel capacity calculated based on the average number of concurrent users and required single-user-perceived throughput barely meets user experience requirements.

At present, the cell-level or network-wide average user-perceived throughput is generally used to evaluate the performance of MBB networks. This covers up some users' dissatisfaction with experience. Therefore, session-level and data-packet-level experience blocking evaluation and related theories are urgently needed.
No mature blocking theory is applicable to MBB networks oriented to user experience. Faced with such problems and challenges, Huawei mLAB, Future Network Theory Lab, and some universities around the world jointly perform related analysis based on live-network data, theoretical analysis, and simulation to formulate the EB table for data services.

The new experience blocking theory for data service networks consists of three parts:

- Call arrival process modeling
- System service abstraction
- Experience blocking evaluation

In the system service model, the system capacity (C) is equal to $\rho \times b$, where $\rho$ is the spectral efficiency (bit/s/Hz), and $b$ is the system bandwidth (Hz). If the required single-user-perceived throughput is $r$ bit/s, the number of equivalent channels (N) is equal to $\rho \times b/r$. Assume that a round robin scheduling policy is used. The call arrival process is modeled at the session and packet levels.

Experience blocking is defined at session and packet levels to indicate the session-level user-perceived throughput satisfaction and packet delay satisfaction, respectively.

- **Session-level experience blocking**
  
  When a user accesses a cell with insufficient capacity (number of equivalent channels), the perceived throughput for concurrent users decreases and it may not be possible to meet experience requirements for all concurrent users.
Traffic Blocking Analysis Methodology

- Hard experience blocking
  The perceived throughput for concurrent users decreases, and the experience requirements of all concurrent users cannot be met. The effect of hard experience blocking can be seen in the degree of video quality degradation for video telephony with a constant code rate, using the UDP protocol.

- Soft experience blocking
  The perceived throughput for concurrent users decreases, and the experience requirements of concurrent users can only be partly met. The effect of soft experience blocking can be seen in the stalling duration ratio for streaming video with a constant code rate, using the TCP protocol.

- Packet delay blocking (packet-level experience blocking)
  When a user accesses a cell with insufficient capacity (number of equivalent channels), packets cannot be scheduled fast enough. The packet delay blocking probability is the probability that the packet delay will exceed a preset target value (for example, 10 ms).

The new traffic blocking theory for data services is an extension of the Erlang B call blocking probability theory. In the new traffic blocking theory for data services, call arrivals following distributions such as Poisson and power-law arrival distributions are considered, and experience blocking is evaluated in terms of session-level hard experience blocking, session-level soft experience blocking, and packet delay blocking. The new traffic blocking theory is designed to analyze the relationships among the traffic volume (A), number of equivalent channels (N), and experience blocking (B).

<table>
<thead>
<tr>
<th>Experience Blocking Analysis Scenario</th>
<th>Call Arrival (Number of Call Arrivals or Interval of Call Arrivals)</th>
<th>Distribution of Call Duration</th>
</tr>
</thead>
<tbody>
<tr>
<td>Experience blocking when call arrivals follow a Poisson distribution (Hard experience blocking, soft experience blocking, and packet delay blocking)</td>
<td>The number of call arrivals in a specified period follows a Poisson distribution.</td>
<td>Exponential distribution</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Power-law distribution</td>
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<tr>
<td></td>
<td>The number of call arrivals in a specified period follows a Poisson distribution.</td>
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<tr>
<td></td>
<td></td>
<td>Power-law distribution</td>
</tr>
<tr>
<td>Experience blocking when call arrivals follow a power-law distribution (Hard experience blocking, soft experience blocking, and packet delay blocking)</td>
<td>The interval of call arrivals follows a power-law distribution.</td>
<td>Exponential distribution</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Power-law distribution</td>
</tr>
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<td>Exponential distribution</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Power-law distribution</td>
</tr>
</tbody>
</table>

Experience blocking analysis scenarios
Based on the call access mode, system service abstraction, and traffic blocking characteristics of data service networks, the following sections provide definitions, calculation methods, theories, and simulation results of session-level experience blocking and packet-level experience blocking. In addition, an EB table is formulated through theoretical analysis and simulation.

**Definition and Calculation Method of Session-level Hard Experience Blocking**

**Definition**
When a user accesses a cell with insufficient capacity (number of equivalent channels), the perceived throughput for all concurrent users decreases and experience requirements for all concurrent users cannot be met.

**Calculation Method**
If the number of concurrent users is greater than the number of equivalent channels in a specified period $t_i$ ($t_i \in [T1, T2]$) within the measurement period $[T1, T2]$, throughput of all concurrent users in $t_i$ cannot meet experience requirements. Hard blocking ratio can be calculated using the following formula:

$$\text{Hard blocking ratio} = \frac{\sum t_i \in [T1, T2] \text{ Unsatisfied traffic volume} [t_i]}{\text{Total traffic volume}}$$

The methods of calculating the satisfied traffic volume and unsatisfied traffic volume in each $t_i$ are as follows:

- Number of concurrent users > Number of equivalent channels
  
  Satisfied traffic volume = 0
  
  Unsatisfied traffic volume = Number of concurrent users

- Number of concurrent users ≤ Number of equivalent channels
  
  Satisfied traffic volume = Number of concurrent users
  
  Unsatisfied traffic volume = 0

The following table provides an example of calculating Hard blocking ratio when the total number of equivalent channels (system capacity) is 10.

<table>
<thead>
<tr>
<th></th>
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<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of concurrent users</td>
<td>10</td>
<td>9</td>
<td>8</td>
<td>7</td>
<td>12</td>
<td>15</td>
<td>16</td>
<td>7</td>
<td>8</td>
<td>9</td>
</tr>
<tr>
<td>Satisfied traffic volume</td>
<td>10</td>
<td>9</td>
<td>8</td>
<td>7</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>7</td>
<td>8</td>
<td>9</td>
</tr>
<tr>
<td>Unsatisfied traffic volume</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>12</td>
<td>15</td>
<td>16</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Hard blocking ratio</td>
<td>0.43</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Example of calculating hard blocking
Traffic Blocking Theory Analysis and Typical Results

Definition and Calculation Method of Session-level Soft Experience Blocking

Definition

When a user accesses a cell with insufficient capacity (number of equivalent channels), the perceived throughput for all concurrent users decreases and experience requirements for concurrent users can be partly met.

Calculation Method

If the number of concurrent users is greater than the number of equivalent channels in a specified period \( t_i \) within the measurement period \([T_1, T_2]\), experience requirements of concurrent users in \( t_i \) can be partly met. Soft blocking ratio can be calculated using the following formula:

\[
\text{Soft blocking ratio} = \frac{\sum_{t_i \in [T_1, T_2]} \text{Unsatisfied traffic volume} [t_i]}{\text{Total traffic volume}}
\]

The methods of calculating the satisfied traffic volume and unsatisfied traffic volume in each \( t_i \) are as follows:

- Number of concurrent users > Number of equivalent channels
  
  Satisfied traffic volume = Number of concurrent users x Actual single-user throughput/Required single-user throughput
  
  Unsatisfied traffic volume = Number of concurrent users x (1 – Actual single-user throughput/Required single-user throughput)

- Number of concurrent users ≤ Number of equivalent channels
  
  Satisfied traffic volume = Number of concurrent users
  
  Unsatisfied traffic volume = 0

The following table provides an example of calculating soft blocking ratio when the total number of equivalent channels (system capacity) is 10.

<table>
<thead>
<tr>
<th></th>
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<th></th>
<th></th>
<th></th>
</tr>
</thead>
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<tr>
<td>Number of concurrent users</td>
<td>10</td>
<td>9</td>
<td>8</td>
<td>7</td>
<td>12</td>
<td>15</td>
<td>16</td>
<td>7</td>
<td>8</td>
<td>9</td>
</tr>
<tr>
<td>Satisfied traffic volume</td>
<td>10</td>
<td>9</td>
<td>8</td>
<td>7</td>
<td>10</td>
<td>10</td>
<td>10</td>
<td>7</td>
<td>8</td>
<td>9</td>
</tr>
<tr>
<td>Unsatisfied traffic volume</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>2</td>
<td>5</td>
<td>6</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Soft blocking ratio</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>0.13</td>
</tr>
</tbody>
</table>

Example of calculating soft blocking

07 White Paper for the Traffic Blocking Theory for Data Services
Traffic Blocking Theory Analysis and Typical Results

### Definition and Calculation Method of Packet Delay Blocking

#### Definition

The packet delay blocking probability is the probability that the packet delay will exceed a preset target value (delay tolerance).

#### Calculation Method

The packet delay blocking probability can be calculated using the following formula:

\[
B_\alpha = \Pr \left[ \frac{\sum_{k=1}^{K} Q_k(\infty)}{C} \geq D \right]
\]

where

- \(Q_k(t)\) is the queue length of the \(k\)th user at the \(t\)th second.
- \(Q_k(\infty)\) is the queue length in the steady state.
- \(C\) is the system capacity.
- \(D\) is delay tolerance.

Delay tolerance probabilities of all users are the same in the steady state because \(K\) queues are symmetric.

---

Assume that the call arrival process model is as follows:

- The number of arrived packets \(N\) in each transmission time interval (TTI) follows the following power-law distribution (Zeta distribution): \(\Pr[N=n]=\frac{(\alpha+1)^{-n}}{\zeta(n)}\), where \(\alpha > 2\) (shape parameter), \(n \geq 0\);
- The size \(L\) of packets follows the following power-law distribution: \(f_L(x) = \beta L_{\text{min}} x^{-\beta-1}\), where \(\beta > 1\) (shape parameter), \(x \geq L_{\text{min}}\).

System parameters are as follows:

- A TTI is \(\tau\) seconds, and the total number of users is \(K\).
- The number of arrived services of the \(k\)th user at time \(t\) is \(N_k(t)\). Lengths of arrived packets are \(L_1(t), L_2(t), \ldots, L_{N_k(t)}(t)\), respectively.
- The spectral efficiency is \(\rho\) bit/s/Hz, and the cell bandwidth is \(b\) Hz. The system capacity \((C)\) is equal to \(\rho \times b\).

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- The spectral efficiency is \(\rho\) bit/s/Hz, and the cell bandwidth is \(b\) Hz. The system capacity \((C)\) is equal to \(\rho \times b\).
Traffic Blocking Theory Analysis and Typical Results

Typical Results of Experience Blocking

According to the preceding definitions, the formula and EB table for the experience blocking theory are formulated for Poisson-distribution call arrivals and power-law-distribution call arrivals through theoretical analysis and simulation.

The following provides the formula for calculating the session-level soft experience blocking ratio for Poisson-distribution call arrivals:

\[
B_s = \frac{\sum_{i=N+1}^{\infty} (i-N) (A)^i}{\sum_{i=1}^{N} A^i + \sum_{i=N+1}^{\infty} \frac{1}{N^i-1}}
\]

where

- \( A \) is the traffic volume. It is equal to \( \lambda x \omega \).
- \( \lambda \) is the average number of call arrivals in a measurement period.
- \( \omega \) is the average call duration in a measurement period.
- \( N \) is the number of equivalent channels.

The following is a session-level soft EB table for Poisson-distribution call arrivals.

<table>
<thead>
<tr>
<th>N/Bs</th>
<th>0.01</th>
<th>0.05</th>
<th>0.1</th>
<th>0.5</th>
<th>1</th>
<th>2</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>0.1236</td>
<td>0.2133</td>
<td>0.2701</td>
<td>0.4694</td>
<td>0.5964</td>
<td>0.7577</td>
</tr>
<tr>
<td>4</td>
<td>0.3262</td>
<td>0.4972</td>
<td>0.5975</td>
<td>0.9219</td>
<td>1.1142</td>
<td>1.3478</td>
</tr>
<tr>
<td>5</td>
<td>0.6123</td>
<td>0.868</td>
<td>1.0118</td>
<td>1.4556</td>
<td>1.7081</td>
<td>2.0069</td>
</tr>
<tr>
<td>6</td>
<td>0.9647</td>
<td>1.3043</td>
<td>1.4899</td>
<td>2.0463</td>
<td>2.3543</td>
<td>2.7125</td>
</tr>
</tbody>
</table>

Example of a session-level soft EB table

The packet delay blocking probability \( (B_d) \) can be calculated using the probability distribution function (PDF) of queue length random variable \( (Q) \) for Poisson-distribution and power-law-distribution packet arrivals. The Laplace-Stieltjes Transform (LST) of the PDF of the queue length random variable \( (Q) \) (approximately) can be described using the following formula:

\[
L_Q(s) = \frac{1 - e^{-Cs}}{1 - \frac{L_A(s)e^{-Cs}}{1 - L_A(s)}}
\]
Experience Blocking Calculation SDK

For industrial and engineering applications, Huawei mLAB launches an application kit for the new traffic blocking theory, including a live-network traffic model analysis and simulation platform, EB table SDK, and related websites.

The following figure provides the input and output parameters of the EB table SDK.

**Input**
Traffic model (Poisson or power-law)
Provide two of the following three parameter values:
- Traffic volume
- Experience blocking ratio
- Number of channels

**EB table SDK**
- Hard blocking
- Soft blocking
- Packet blocking

**Output**
Get the other one of the following three parameter values:
- Traffic volume
- Experience blocking ratio
- Number of channels

Example of a packet delay blocking table

When this table is used in a typical service scenario, the number of equivalent channels (N) in a system can be calculated based on the system capacity and the typical rate of the service.

The traffic volume (A) is a normalized value for the required service duration in a specified period.

### Relationship Among the Packet Delay Blocking Probability (Bd, Unit: %), Number of Channels (N), and Traffic Volume (A)

<table>
<thead>
<tr>
<th>N/A</th>
<th>0.01</th>
<th>0.05</th>
<th>0.1</th>
<th>0.5</th>
<th>1</th>
<th>2</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>0.0034</td>
<td>0.0035</td>
<td>0.0036</td>
<td>0.0043</td>
<td>0.0047</td>
<td>0.0102</td>
</tr>
<tr>
<td>4</td>
<td>0.0038</td>
<td>0.0039</td>
<td>0.0053</td>
<td>0.0091</td>
<td>0.0249</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>0.0041</td>
<td>0.0046</td>
<td>0.0048</td>
<td>0.0096</td>
<td>0.0178</td>
<td>0.0471</td>
</tr>
<tr>
<td>6</td>
<td>0.0069</td>
<td>0.0072</td>
<td>0.0076</td>
<td>0.0111</td>
<td>0.0238</td>
<td>0.1434</td>
</tr>
</tbody>
</table>

where

\( L_A(s) \) is the LST of the packet arrival process.

\( s \) is a complex number.

\( C \) is the system capacity.

\( \theta \) is the idle rate of the system.

The following is a packet delay blocking table (target packet delay: 10 ms) for power-law-distribution packet arrivals.
The EB table can be used to evaluate the experience blocking status of users in the system based on system capacity, traffic modeling, and single-user bandwidth requirements. It can also be used to plan system channel capacity through theoretical analysis and simulation according to the experience blocking targets.

**Application 1: System Capacity Adjustment Method Based on Traffic Volume Requirements**

The method of adjusting system capacity based on traffic volume requirements is as follows:

- Assume that:
  - The spectral efficiency is $\rho$ bit/s/Hz.
  - The cell bandwidth is $b$ Hz.
  - The required single-user throughput is $r$ bit/s.
  - The number of equivalent channels ($N$) in a cell is $\rho \times b/r$.
- Query the maximum traffic volume ($A'$) supported by the cell in the EB table when target experience blocking ($B'$) and the number of equivalent channels ($N$) are specified.
- Calculate the currently required traffic volume ($A$) based on the currently required single-user throughput and the total data volume in the system.
Traffic Blocking Theory Application

- Determine whether to adjust system capacity based on the relationship between $A$ and $A'$:
  - Retain system capacity if $A$ is less than or equal to $A'$.
  - Adjust system capacity if $A$ is greater than $A'$.
- Query the number of equivalent channels ($N'$) to be adjusted based on the currently required traffic volume ($A$) and target experience blocking ($B'$) if the system capacity needs to be adjusted.

### Application 2: System Capacity Adjustment Method Based on Experience Blocking Analysis

The method of adjusting system capacity based on experience blocking analysis of the system logs is as follows:

- Measure user-perceived throughput in each session, and obtain the current experience blocking ($B$) based on the required single-user throughput.
- Obtain the number of equivalent channels ($N$) in a cell based on the current spectral efficiency, cell bandwidth, and required single-user throughput in the cell.
- Determine whether to adjust system capacity based on the relationship between $B$ and target experience blocking ($B'$):
  - Retain system capacity if $B$ is less than or equal to $B'$.
  - Adjust system capacity if $B$ is greater than $B'$.
- Query the number of equivalent channels ($N'$) to be adjusted based on the currently required traffic volume ($A$) and target experience blocking ($B'$) if the system capacity needs to be adjusted.

### Future Development

In the future, Huawei mLAB will establish a live-network traffic model analysis and simulation platform and launches the EB table SDK and related websites. In addition, Huawei mLAB will work with operators and other experts, supporting studies and other projects, to constantly optimize and improve this theory.

For more information, contact Huawei mLAB personnel at mbblab@huawei.com
X Labs is a brand-new platform designed to get together telecom operators, technical vendors and partners from vertical sectors to explore future mobile application scenarios, drive business and technical innovations and build an open ecosystem. X Labs have set up three laboratories, which aim to explore three major areas: people-to-people connectivity, applications for vertical sectors and applications in household.